

George Berkeley (1685-1753):

Esse est percipi.

To be is to be perceived.

HR: **observation of an event :=**
interaction that occurs

if and only if the event takes place.

exist := being observable, able to interact;

fact := a verifiabl{y|e} observed phenomenon;

reality := *all* that exists; the entirety of *all* facts
(i.e. observable & observed reality).

There exists no observational evidence of anything unobservable.

Physics is about reality & not about brainchildren.

"Existance postulate":

An entity cannot exist unless it is able to fully manifest all of its properties.

Based on common sense, essentially refines definition of exist.

- An entity having any spatial property requires
- a minimal amount of space in order to exist.

An entity having *mass* has at least two spatial properties: its *Schwarzschild radius* and its *Compton wavelength*.

- **A *mass* requires more than zero space in order to exist.**
- We could (re)define ***size*** as this minimally required space.

Schwarzschild volume = sphere with diameter = $2r_S$:

$$V_S = \frac{4\pi}{3} r_S^3 = \frac{4\pi}{3} \left(\frac{2GM}{c^2} \right)^3 = \frac{4\pi}{3} \cdot \frac{8G^3 M^3}{c^6} = \frac{32\pi G^3 M^3}{3c^6}$$

Compton volume = sphere with diameter = λ_C ("Compton dipole"):

$$V_C = \frac{4\pi}{3} \left(\frac{\lambda_C}{2} \right)^3 = \frac{4\pi}{3} \cdot \frac{h^3}{8m^3 c^3} = \frac{\pi h^3}{6m^3 c^3}$$

Tipping point: $V_S = \frac{32\pi G^3 m_{SC}^3}{3c^6} = \frac{\pi h^3}{6m_{SC}^3 c^3} = V_C$

$$\therefore \frac{32\pi G^3 m_{SC}^3 \cdot 6m_{SC}^3 c^3}{3c^6 \cdot \pi h^3} = 1 \therefore \frac{64G^3 m_{SC}^6}{c^3 h^3} = 1 \therefore m_{SC}^6 = \frac{c^3 h^3}{4^3 G^3}$$

$$\therefore m_{SC} = \sqrt{\frac{ch}{4G}} \approx 27.27756 \quad \mu\text{g} \quad (\text{CODATA 2018}).$$

$$\Delta l_{SC} = \frac{h}{cm_{SC}} = \frac{h\sqrt{4G}}{c\sqrt{ch}} = \sqrt{\frac{4hG}{c^3}} \approx 8.102701 \times 10^{-35} \text{ m}$$

$$\Delta t_{SC} = \frac{\Delta l_{SC}}{c} \approx 2.702770 \times 10^{-43} \text{ s}$$

Seems more fundamental than Planck mass & length.

But Schwarzschild-Compton density & pressure

seem hilariously laughably ridiculously gargantuan:

$$\begin{aligned} \rho_{SC} &= \frac{m_{SC}}{V_{SC}} = \frac{m_{SC}}{\pi h^3 / 6 m_{SC}^3 c^3} = \frac{6 m_{SC}^4 c^3}{\pi h^3} = \frac{6 \sqrt{\frac{ch}{4G}}^4 c^3}{\pi h^3} = \frac{6 \frac{c^2 h^2}{4^2 G^2} c^3}{\pi h^3} = \frac{6 c^2 h^2 c^3}{16 \pi h^3 G^2} \\ &= \frac{3 c^5}{8 \pi h G^2} \approx 9.793038 \times 10^{94} \text{ kg/m}^3 \end{aligned}$$

$$p_{SC} := \rho_{SC} \cdot c^2 \approx 8.801543 \times 10^{111} \text{ Pa.}$$

Diameters of proton (1.6826 fm) & neutron (~1.6 fm) slightly exceed their respective Compton wavelengths (1.3214 fm & 1.3196 fm).

Compton density & pressure of proton (the only stable baryon):

$$\rho_{C,p} := \frac{m_p}{V_{C,p}} = \frac{m_p}{\pi h^3 / 6m_p^3 c^3} = \frac{6m_p^4 c^3}{\pi h^3} \approx 1.3845 \times 10^{18} \text{ kg/m}^3$$

$$p_{C,p} := \rho_{C,p} \cdot c^2 \approx 1.2443 \times 10^{35} \text{ Pa}$$

(neutron: $1.3921 \times 10^{18} \text{ kg/m}^3$ & $1.2512 \times 10^{35} \text{ Pa}$).

Do you know the **observed** internal pressure of a proton?

It is of $\mathcal{O}(10^{35} \text{ Pa})$ ^[1]

Even strong nuclear force does not crush nucleons inside atomic nucleus, does it?

At neutron Compton density, m_{SC} would have a diameter of $\sim 3.345 \text{ nm}$.

¹ Burkert, V.D., Elouadrhiri, L. & Girod, F.X. The pressure distribution inside the proton. *Nature* **557**, 396-399 (2018).